



K23U 2365

Reg. No. :

Name :

V Semester B.Sc. Degree (C.B.C.S.S. – O.B.E. – Regular/Supplementary/
Improvement) Examination, November 2023

(2019-2021 Admissions)

CORE COURSE IN MATHEMATICS

5B05 MAT : Set Theory, Theory of Equations and Complex Numbers

Time : 3 Hours

Max. Marks : 48

PART – A

Answer **any 4** questions from this part. **Each** question carries **1** mark. **(4×1=4)**

1. Give example for a denumerable set.
2. If α, β, γ are the root of the equation $f(x) = 0$, then the equation whose roots are $-\alpha, -\beta, -\gamma$ is _____
3. Show that $x^5 - 2x^2 + 7 = 0$ has atleast two imaginary roots.
4. If ω is an imaginary cube root of unity, then the value of $1 + \omega + \omega^2$ is _____
5. What is the value of $\text{Arg } z$ for positive real axis, $z = x$?

PART – B

Answer **any 8** questions from this part. **Each** question carries **2** marks. **(8×2=16)**

6. Show that the set of all integers is countable.
7. If α, β, γ are the root of the equation $ax^3 + bx^2 + cx + d = 0$, then find the values of $\alpha + \beta + \gamma$ and $\alpha\beta\gamma$.
8. Find the condition that the cubic equation $x^3 - lx^2 + mx - n = 0$ should have its roots in arithmetical progression.
9. If α, β, γ are the root of the equation $8x^3 - 4x^2 + 6x - 1 = 0$, find the equation whose roots are $2\alpha + 1, 2\beta + 1, 2\gamma + 1$.
10. State De Gua's rule.
11. What do you mean by reciprocal equation ? Give an example.

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12. Describe the discriminant of the cubic equation $ax^3 + 3bx^2 + 3cx + d = 0$.
13. Transform $x^3 - 6x^2 + 5x + 12 = 0$ into an equation lacking the second term.
14. If a, b, c are the roots of the cubic equation $x^3 + px^2 + qx + r = 0$, find the value of $\frac{1}{a^2b^2} + \frac{1}{b^2c^2} + \frac{1}{c^2a^2}$.
15. What are the imaginary cube root of unity ?
16. Find the polar form of $z = 1 + i$.

PART – C

Answer **any 4** questions from this part. **Each** question carries **4** marks. **(4×4=16)**

17. If A is a set with m elements and B is a set with n elements and if $A \cap B = \phi$, then prove that $A \cup B$ has $m + n$ elements.
18. Solve the equation $x^4 - 2x^3 + 4x^2 + 6x - 21 = 0$, given that the sum of the two of its roots is zero.
19. Find the rational roots of $x^4 - 39x^2 + 46x - 168 = 0$.
20. Solve $6x^5 + 11x^4 - 33x^2 + 11x + 6 = 0$.
21. Describe the behaviour of roots of a cubic equation in terms of its discriminant.
22. Find the value of $\sqrt{1+i}$.
23. Find the fifth root of (-1) .

PART – D

Answer **any 2** questions from this part. **Each** question carries **6** marks. **(2×6=12)**

24. State and prove Cantor's theorem.
25. If α, β, γ are the root of the equation $ax^3 + 3bx^2 + 3cx + d = 0$, then find the values of
- $(\alpha^2 + 1) (\beta^2 + 1) (\gamma^2 + 1)$
 - $(\beta - \gamma) (\gamma - \alpha) + (\gamma - \alpha) (\alpha - \beta) + (\alpha - \beta) (\beta - \gamma)$.
26. Find a real root of the $x^3 + x^2 - 16x + 20 = 0$.
27. If z_1 and z_2 are two complex numbers, prove that
- $|z_1 z_2| = |z_1| |z_2|$
 - $\arg(z_1 z_2) = \arg z_1 + \arg z_2$.