

K24P 1109

Reg. No. :

Name :

Second Semester M.Sc. Degree (C.B.C.S.S. – OBE-Regular) Examination, April 2024 (2023 Admission) PHYSICS MSPHY02C08/MSPHN02C08 : Quantum Mechanics – 1

SECTION – A

Time : 3 Hours

Max. Marks : 60

Answer any five questions, each carry 3 marks.

- 1. Compare the classical and quantum speeds of a free particle.
- 2. Write three properties of projection operator.
- 3. Evaluate [X, Lx], [Y, Ly] and [Z, Lz].
- 4. Write three points to distinguish between bosons and fermions.
- 5. What is Clebsch-Gordan coefficients ?
- 6. Write and explain three conservation laws and their corresponding symmetries.

(5×3=15)

SECTION – B

Answer any three questions, each carry six marks.

- 7. For a Harmonic Oscillator derive the equation $(a_+ a_- + \frac{1}{2} \hbar \omega) \psi = E \psi$.
- 8. Explain the terms linearly dependent and linearly independent. Check whether the functions f(x) = x, g(x) = 5x, $h(x) = x^4$ are linearly independent.
- 9. Prove any three properties of Pauli's spin Matrixes.

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- 10. Two non-interacting particles are placed in an infinite square well. Their one particle states are given by $\psi_n(x) = (2/a)^{1/2} \operatorname{Sin}(n\pi x/a)$, with energy = n²K, where K is a constant. Write the composite wave function.
 - 1) If the particles are distinguishable
 - 2) If the particles are bosons
 - 3) If the particles are fermions.
- For an infinite square well, define the potential, write the Schrodinger equation, solve it in different regions of potential. (3×6=18)

Answer any three questions, each carry 9 marks.

- 12. Solve the harmonic oscillator problem with analytic method.
- 13. Explain the basics of a Linear vector space and explain how it is related to Hilbert space.
- 14. Derive the relations
 - 1) $J^{2}|j, m > = \hbar^{2} j(j + 1)|j, m >$
 - 2) J_{z} |j, m > = \hbar m| j, m > and
 - 3) $J_{\pm} |j, m \rangle = \hbar [j(j \pm 1) m (m \pm 1)]^{1/2} |j, m \pm 1 \rangle$.
- 15. Discuss in detail the conservation laws behind the displacement in space, rotations in space and displacement in time.
- 16. Discuss the infinite square well problem, find the energy and normalized wavefunction. (3×9=27)

